

COMBINATORICS  
SEMINAR

*Crossing and Color*

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**Abstract:** Turán defined  $cr(G)$ , the crossing number of a graph  $G$ , as the smallest number of edge crossings in a proper drawing of  $G$  in the plane. This notion has turned out to play an important role in combinatorial geometry, additive number theory, chip design, and elsewhere. The computation of  $cr(G)$  is a classical NP-hard problem, so it is not surprising that there are very few graphs whose crossing numbers are known. In particular, we do not even know the asymptotic value of the crossing number of the complete graph  $K_r$  on  $r$  vertices, as  $r$  tends to infinity. Nevertheless, Albertson made the conjecture that  $cr(G)$  is at least  $cr(K_r)$ , for any graph  $G$  whose chromatic number is at least  $r$ . After giving a short and biased survey of some important results on crossing numbers, we explain the relationship between crossings and coloring, and settle Albertson's conjecture for graphs whose number of vertices is not much larger than their chromatic number. Joint work with Jacob Fox and Andrew Suk.

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