## Math 421 Problem Set November 10, 2022

1. Recall that the alternating group $A_{4} \leq S_{4}$ is the subgroup consisting of even permutations.
(a) List all elements of $A_{4}$ and find their orders.
(b) Show that $A_{4}$ is not isomorphic to $D_{12}$.
(c) Show that $A_{4}$ has exactly one subgroup $H$ of order 4 and $H \cong Z_{2} \times Z_{2}$.
(d) Use a problem from last week's homework to conclude that $H \unlhd A_{4}$.
