## Math 421 Problem Set November 10, 2022

- 1. Recall that the alternating group  $A_4 \leq S_4$  is the subgroup consisting of even permutations.
  - (a) List all elements of  $A_4$  and find their orders.
  - (b) Show that  $A_4$  is not isomorphic to  $D_{12}$ .
  - (c) Show that  $A_4$  has exactly one subgroup H of order 4 and  $H \cong Z_2 \times Z_2$ .
  - (d) Use a problem from last week's homework to conclude that  $H \leq A_4$ .