

1. [1 point] How many elements are in  $A_4$ ? No explanation needed.

12

2. [1 point] Give an explicit example of a (non-trivial) element of  $A_4$ .

$$(12)(34)$$

3. [1 point] Give an explicit example of an element of  $S_4$  that is not in  $A_4$ .

$$(12)$$

4. [2 points] Set  $H \leq A_4$  to be the unique subgroup of order 4. To which familiar group is  $(S_4/H)/(A_4/H)$  isomorphic? Briefly explain.

$$(S_4/H)/(A_4/H) \cong S_4/A_4 \text{ by the 3rd Isomorphism Theorem.}$$

$$|S_4/A_4| = 2, \text{ so it's isomorphic to } \mathbb{Z}/2\mathbb{Z}, \text{ (or } \mathbb{Z}_2\text{.)}$$