

# Math 362: Mathematical Statistics II

Le Chen

le.chen@emory.edu

Emory University  
Atlanta, GA

Last updated on April 13, 2021

2021 Spring

# Chapter 6. Hypothesis Testing

§ 6.1 Introduction

§ 6.2 The Decision Rule

§ 6.3 Testing Binomial Data –  $H_0 : p = p_0$

§ 6.4 Type I and Type II Errors

§ 6.5 A Notion of Optimality: The Generalized Likelihood Ratio

# Plan

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Instead of numerical estimates of parameters, in the form of either single points or confidence intervals, we want to make a choice between two conflicting theories, or **hypothesis**:

1.  $H_0$ :  $\mu = \mu_0$
2.  $H_1$ :  $\mu \neq \mu_0$

Comments: Hypothesis testing and confidence intervals are dual concepts to each other:

- ▶ Confidence intervals are point estimates of  $\mu$  with margin of error
- ▶ Hypothesis testing is point estimates of  $\mu$  with margin of error

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