## Algebra Seminar

Polynomials non-negative on non-compact semialgebraic sets

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**Abstract:** Recently, M. Marshall answered a long-standing question in real algebraic geometry by showing that if  $f(x, y) \in \mathbf{R}[x, y]$  and  $f(x, y) \ge 0$  on the strip  $[0, 1] \times \mathbf{R}$ , then f has a representation  $f = \sigma_0 + \sigma_1 x (1 - x)$ , where  $\sigma_0, \sigma_1 \in \mathbf{R}[x, y]$  are sums of squares.

In this talk, we give the background to this result, which goes back to Hilbert's 17th problem, and our generalizations to other non-compact basic closed semialgebraic sets of  $\mathbf{R}^2$  which are contained in strip. We also give some negative results.

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## MATHEMATICS AND COMPUTER SCIENCE EMORY UNIVERSITY