SIAM STUDENT CHAPTER SEMINAR

Weakly quasirandom hypergraphs

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Abstract: We consider quasi-random properties of k-uniform hypergraphs. The central notion is uniform edge distribution with respect to large vertex sets. We find several equivalent characterisations of this property and this work can be viewed as a natural extension of the well known Chung-Graham-Wilson theorem for quasi-random graphs.

Those characterisation for hypergraphs have an interesting consequence for the theory of quasirandom graphs. Let K_k be the complete graph on k vertices and let M(k) be the line graph of the graph of the k-dimensional hypercube. We show that the pair of graphs $(K_k, M(k))$ has the following property: if the number of copies of both K_k and M(k) in another (large) graph G are as expected in the random graph of density d, then G is quasi-random (in the sense of the Chung-Graham-Wilson theorem) with density close to d. Those pairs of non-bipartite graphs with this property.

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This is joint work with D. Conlon, H. Han, and Y. Person.

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