## Algebra and Number Theory Seminar

Tensor products of division algebras

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Abstract: If F is algebraically closed, and  $F_i \supset F$  are field extensions, then  $F_1 \otimes_F F_2$  is always a domain. It thus makes sense to conjecture that if  $D_i/F_i$  are division algebras (meaning  $F_i$  is the center of  $D_i$  and  $D_i/F_i$  is finite dimensional), then  $D_1 \otimes_F D_2$  is a (noncommutative) domain. We will show that this is often true, but not always. We will concentrate on the case that F has characteristic 0 and that the  $D_i/F_i$  have prime degree. We also hope to draw attention to the interesting properties of  $F_1 \otimes_F F_2$  and how they relate to our problem. Along the way we will make use of Picard varieties and elliptic curves.

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