# Number Theory <br> SEminar 

# The degrees of divisors of $x^{n}-1$ 

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#### Abstract

We discuss what is known about the following questions concerning the degrees of divisors of $x^{n}-\operatorname{in} Z[x]$, as n ranges over the natural numbers:


1. How often does $x^{n}-1$ have AT LEAST ONE divisor of every degree between 1 and $n$ ?
2. How often does $x^{n}-1$ have AT MOST ONE divisor of every degree between 1 and $n$ ?
3. How often does $x^{n}-1$ have EXACTLY ONE divisor of every degree between 1 and $n$ ?
4. For a given $m$, how often does $x^{n}-1$ have a divisor of degree $m$ ?

We will also discuss what changes when Z is replaced by the finite field $F_{p}$. A portion of this talk is based on joint work with Paul Pollack.

Wednesday, February 6, 2013, 3:00 pm
Mathematics and Science Center: W306

