

ALGEBRA  
SEMINAR

*Equivariant analogs of the arithmetic of del Pezzo surfaces*

Alexander Duncan  
University of South Carolina

**Abstract:** Given an algebraic variety  $X$  over a non-closed field, one might ask if  $X$  is rational, is unirational, has a rational point, has a Zariski-dense set of rational points, or has a 0-cycle of degree 1. All of these properties have “equivariant” generalizations to the case where the variety has an action of algebraic group  $G$ . The corresponding properties are interesting even when the base field is algebraically closed. Moreover, one can exploit this connection to establish geometric facts using arithmetic methods and vice versa.

I will outline this correspondence with an emphasis on del Pezzo surfaces. In particular, I will completely characterize the equivariant analogs of the above properties for del Pezzo surfaces of degree greater than or equal to 3 over the complex numbers. I will also discuss some partial results for degrees 1 and 2 that, despite being about complex surfaces, have arithmetic ramifications

Tuesday, April 4, 2017, 5:00 pm  
Mathematics and Science Center: W306

MATHEMATICS AND COMPUTER SCIENCE  
EMORY UNIVERSITY