# Dissertation 

DEfEnSE

## On Pisier type problems

Marcelo Sales<br>Emory University

Abstract: A subset $A$ of integers is free if for every two distinct subsets $B, B^{\prime} \subset A$ we have

$$
\sum_{b \in B} b \neq \sum_{b^{\prime} \in B^{\prime}} b^{\prime} .
$$

Pisier asked if, for every subset $A$ of integers, the following two statements are equivalent:
(1) $A$ is a union of finitely many free sets.
(2) There exists $\epsilon>0$ such that every finite subset $B \subset A$ contains a free subset $C \subset B$ with $|C| \geq \epsilon|B|$.

In a more general framework, the Pisier question can be seen as the problem of determining if statements (1) and (2) are equivalent for subsets of a given structure with the prescribed property. We study the problem for several structures including $B_{h}$-sets, arithmetic progressions, independent sets in hypergraphs, and configurations in the euclidean space.

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Advisor: Vojtech Rodl

## Mathematics Emory University

