Algebra and Number Theory Seminar

On the stable birationality of Hilbert schemes of points on surfaces

Morena Porzio Columbia University

Abstract: The Cassels–Swinnerton-Dyer conjecture says that cubic surfaces of index 1 have a rational point. This can be reformulated into a statement about the existence of rational maps between Hilbert schemes of points Hilb_X^n , which in turn motivates the study of the stable birational type of Hilb_X^n . In this talk, we will address the question for which pairs of integers (n, n') the variety Hilb_X^n is stably birational to Hilb_X^n , when X is a surface with $H^1(X, \mathcal{O}_X) = 0$. In order to do so we will relate the existence of degree n' effective cycles on X with the existence of degree n ones using curves on X. We will then focus on geometrically rational surfaces, proving that there are finitely many birational classes among Hilb_X^n 's.

Tuesday, November 19, 2024, 5:00 pm Mathematics and Science Center: MSC W303

> MATHEMATICS EMORY UNIVERSITY